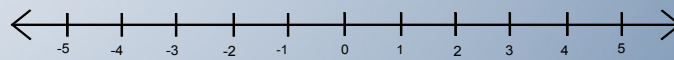
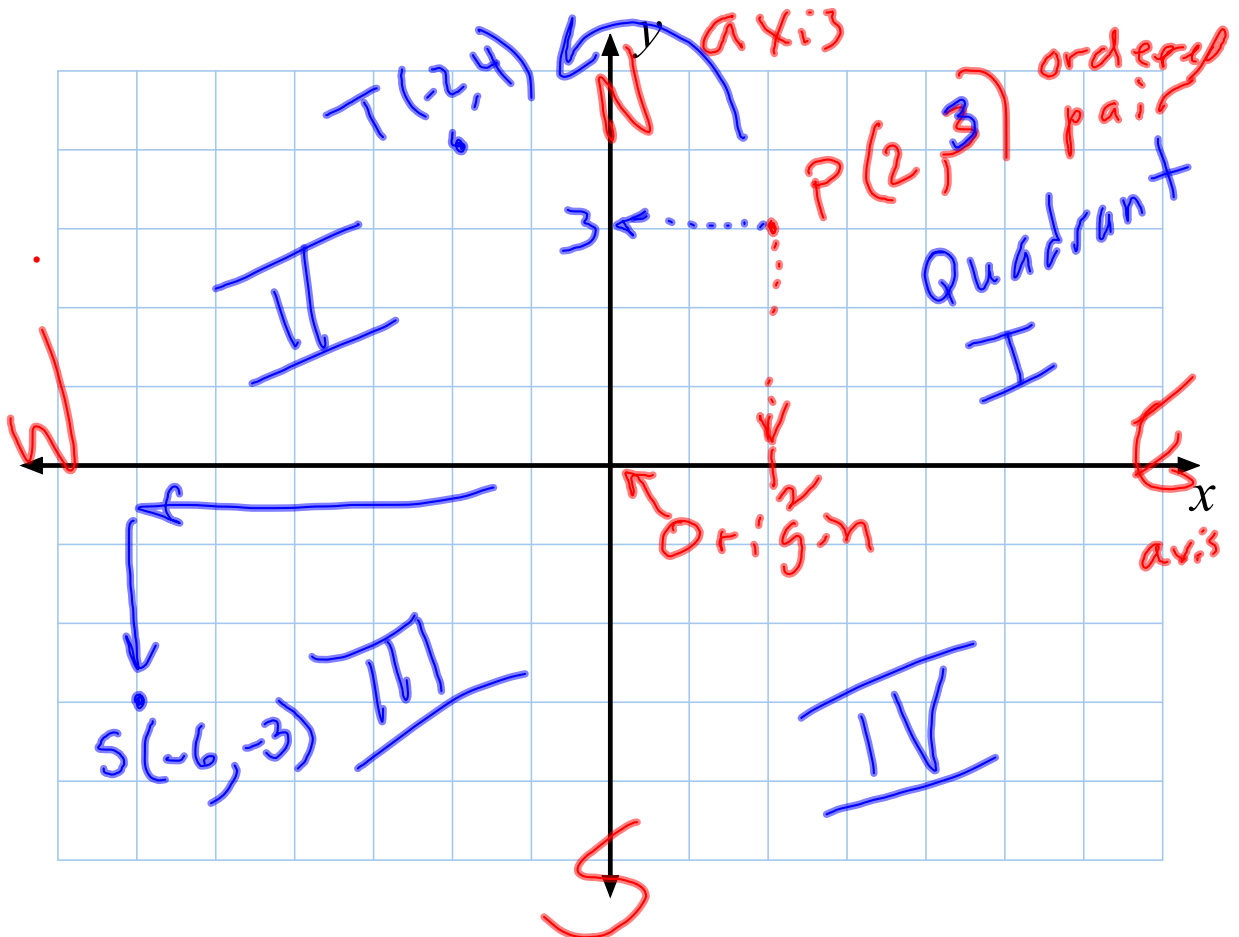
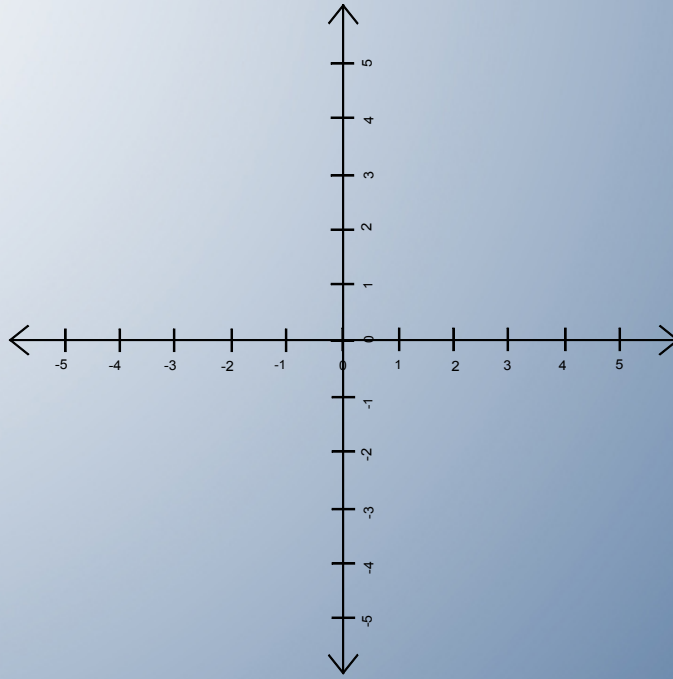
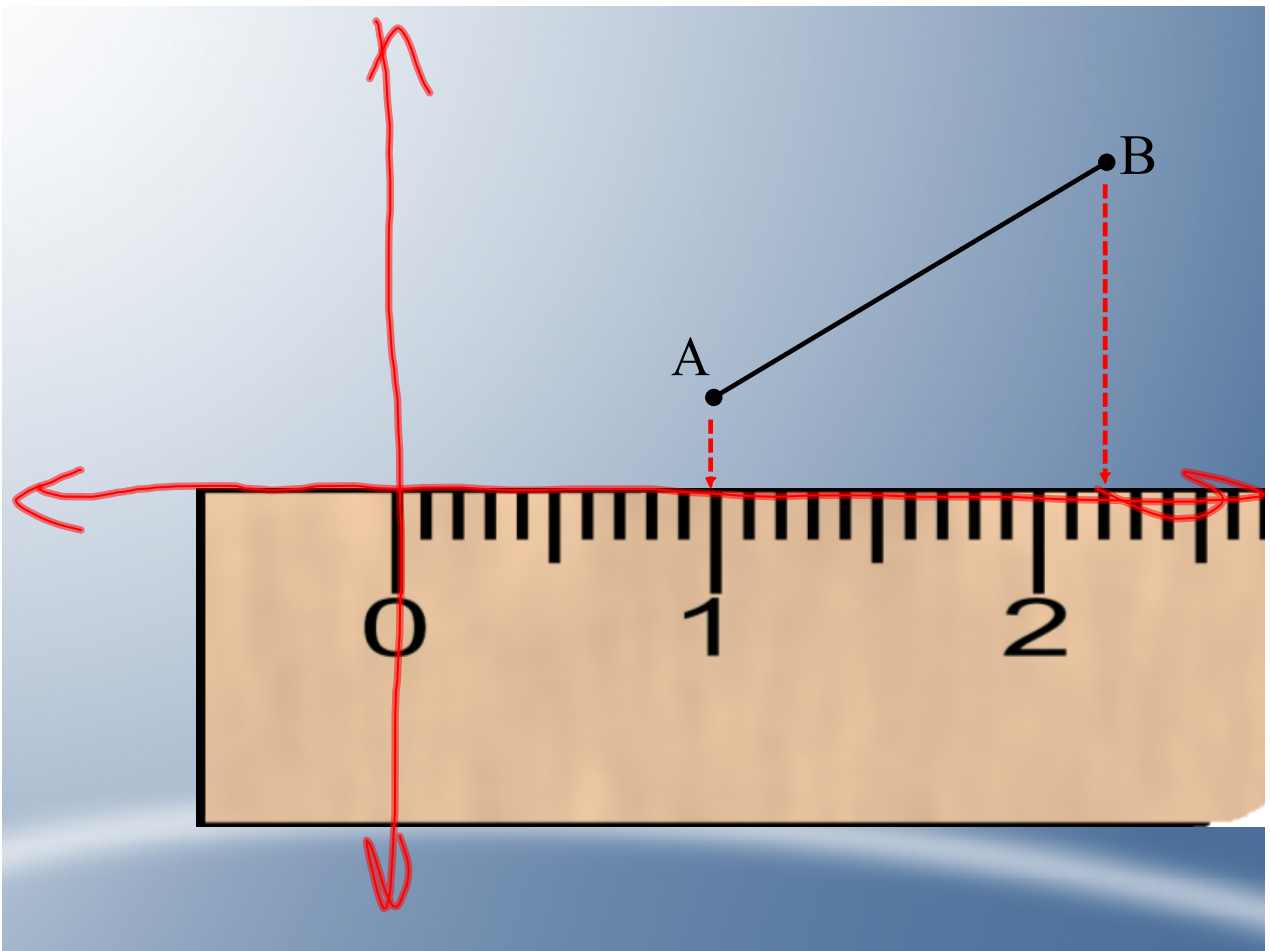
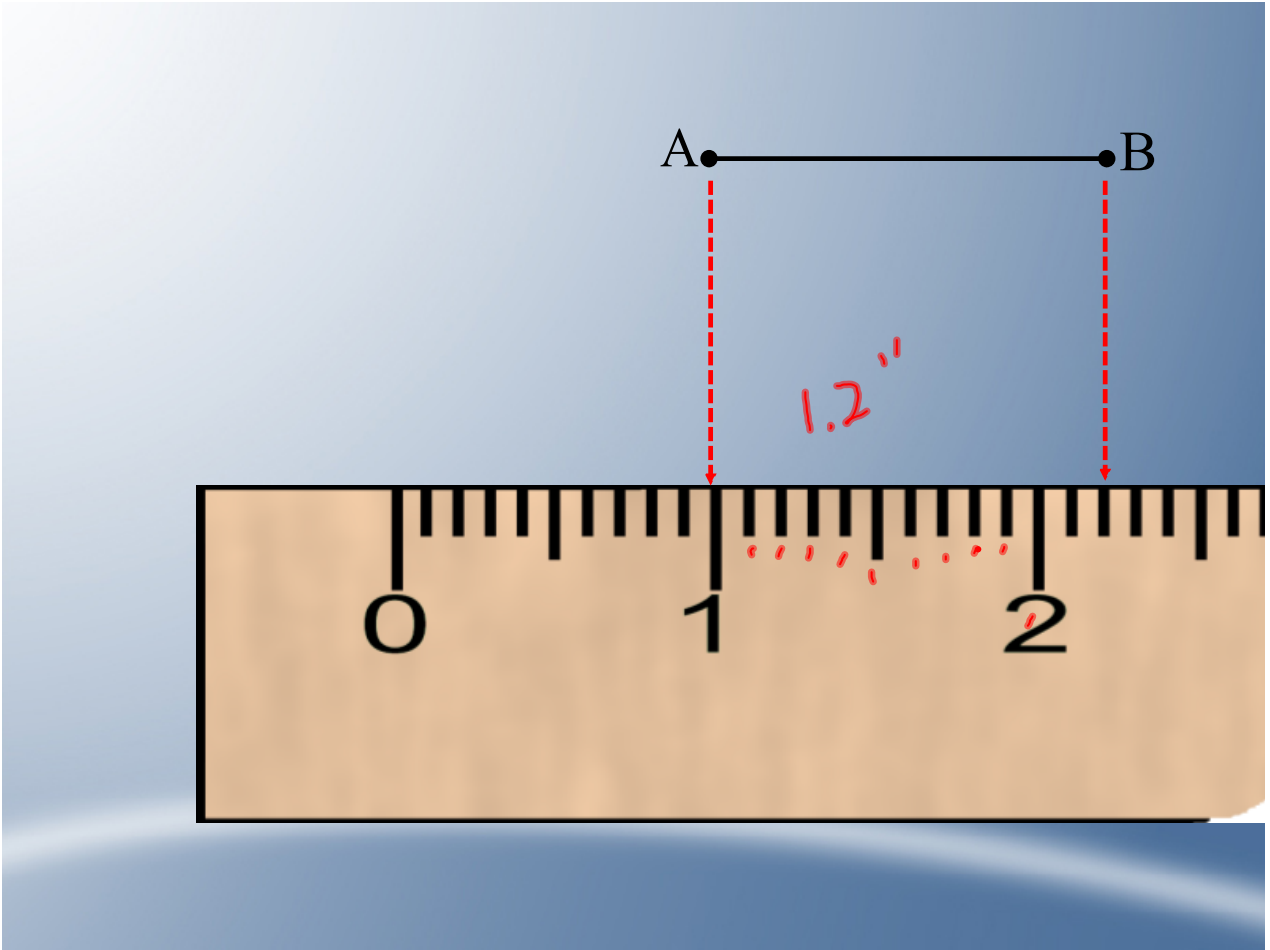


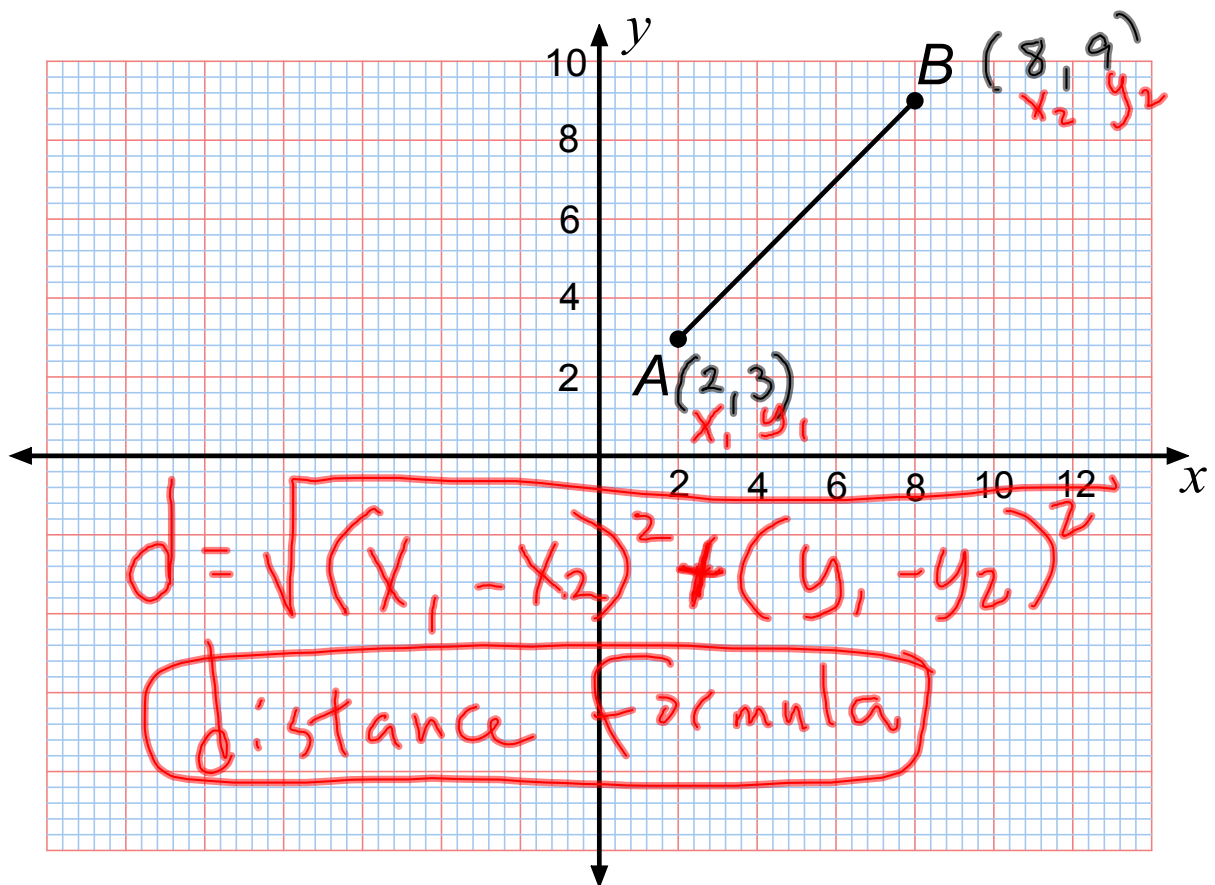
René Descartes

- ~ 1600's
- Invented the Cartesian coordinate system after watching a fly buzz around the ceiling









Example (pg 46 #6)

$$E \begin{pmatrix} 6 \\ x_1 \\ -2 \\ y_1 \end{pmatrix}$$

$$P \begin{pmatrix} -2 \\ x_2 \\ 4 \\ y_2 \end{pmatrix}$$

$$\begin{aligned}
 d &= \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2} \\
 &= \sqrt{(6 - (-2))^2 + (-2 - 4)^2} \\
 &= \sqrt{(8)^2 + (-6)^2} \\
 &= \sqrt{64 + 36} \\
 &= \sqrt{100} = 10
 \end{aligned}$$

$$B \begin{pmatrix} -4 \\ -5 \end{pmatrix} \\ \begin{matrix} x_1 \\ y_1 \end{matrix}$$

$$C \begin{pmatrix} 5 \\ 8 \end{pmatrix} \\ \begin{matrix} x_2 \\ y_2 \end{matrix}$$

$$d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

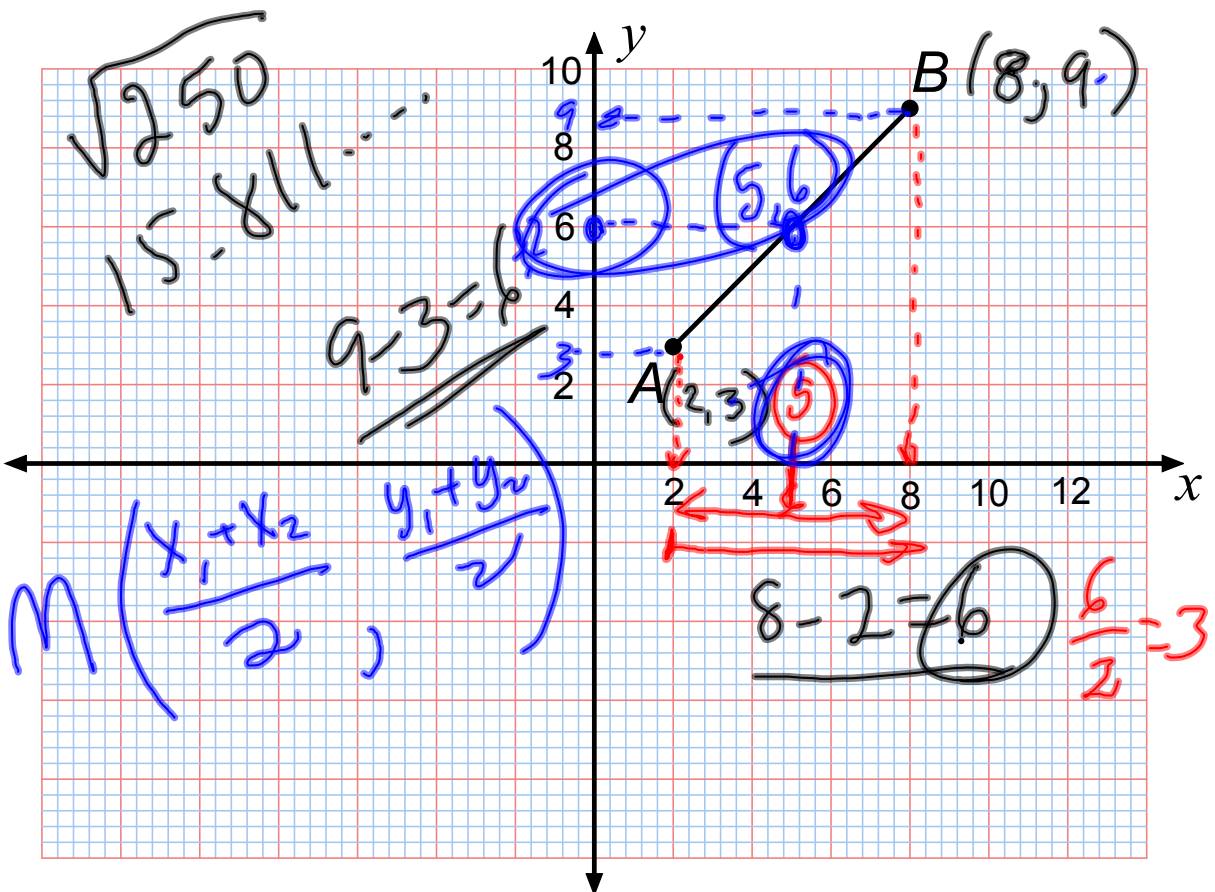
$$d = \sqrt{(-4 - 5)^2 + (-5 - 8)^2}$$

$$\sqrt{(-9)^2 + (-13)^2}$$

$$\sqrt{81 + 169}$$

$$\sqrt{250} = 15.811$$

$$d = 15.8$$



The midpoint formula

The midpt M of AB with endpts $A(x_1, y_1)$ and $B(x_2, y_2)$ is:

$$M \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

Example (pg 46 #20)

$$H(x_1, y_1)$$

$$X(x_2, y_2)$$

$$M \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

$$(3.5, 1)$$

#24 (10, -20)

M $\left(\frac{4+y_2}{2}, \frac{4+y_2}{2} \right)$

(x, y)
 $(0, 4)$

M (5, -8)

$$2(5) = \frac{4+y_2}{2}$$
$$10 = \frac{4+y_2}{2}$$
$$4+y_2 = (-8) \cdot 2$$
$$4+y_2 = -16$$
$$-4 \quad -4$$

$$y_2 = -20$$

$$3 \left(\frac{x}{3} \right)$$
$$\frac{x+1}{3}$$

x+1